

# Tidal Energy and the 18.6 Year Cycle in the Bering Sea

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## **Outline:**

- *Background*
- *Tidal model & inverse*
- *Energy fluxes and dissipation*
- *18.6 year cycle*
- *Summary*

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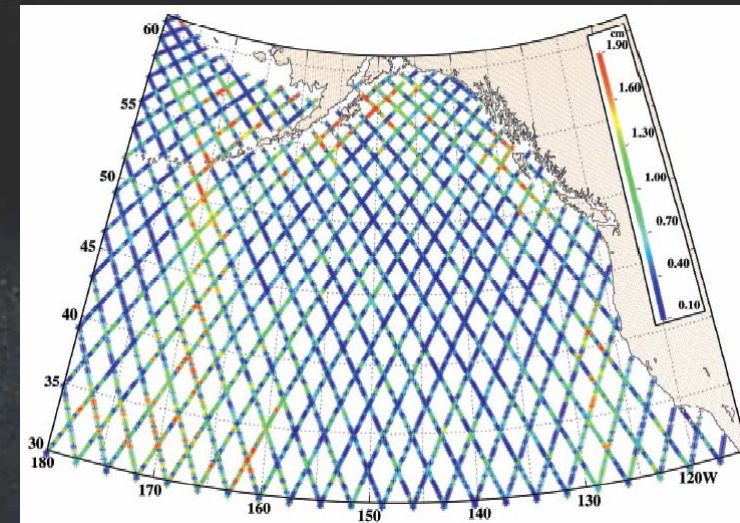
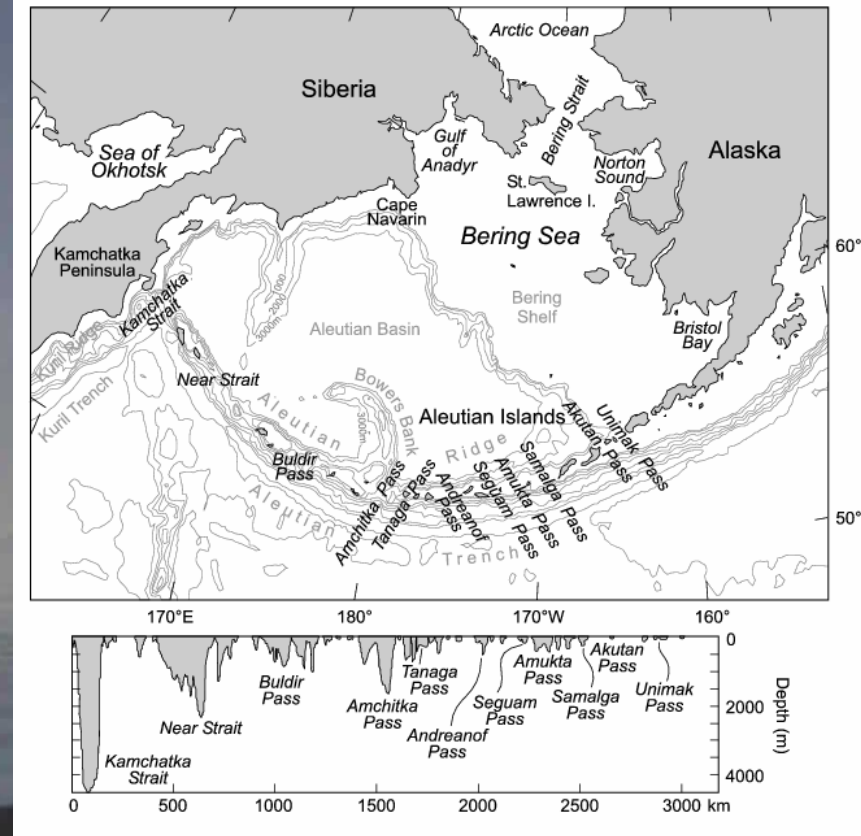
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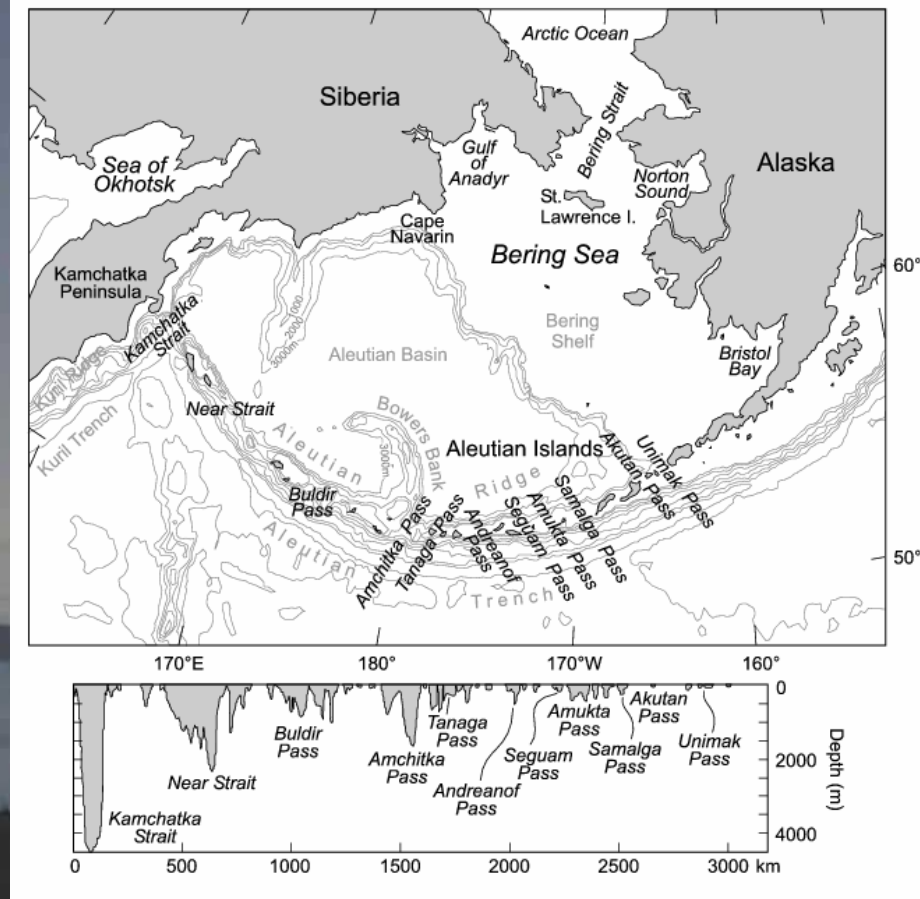
# Background & Motivation

- complex tidal elevations & flows in the Bering Sea
  - Large elevation ranges in Bristol Bay
  - Large currents in the Aleutian Passes
  - both diurnal & semi-diurnal amphidromes
  - Large energy dissipation (Egbert & Ray, 2000)
  - Interactions with seasonal ice cover
  - Internal tide generation from Aleutian passes (Cummins et al., 2001)



# Background & Motivation

- Wide shelf, complex bathymetry, narrow entrances
- Relatively large diurnal currents that will have 18.6 year modulations
- Difficult to get currents & energy balance right with only a forward model
- Need to incorporate observations
  - Data assimilation



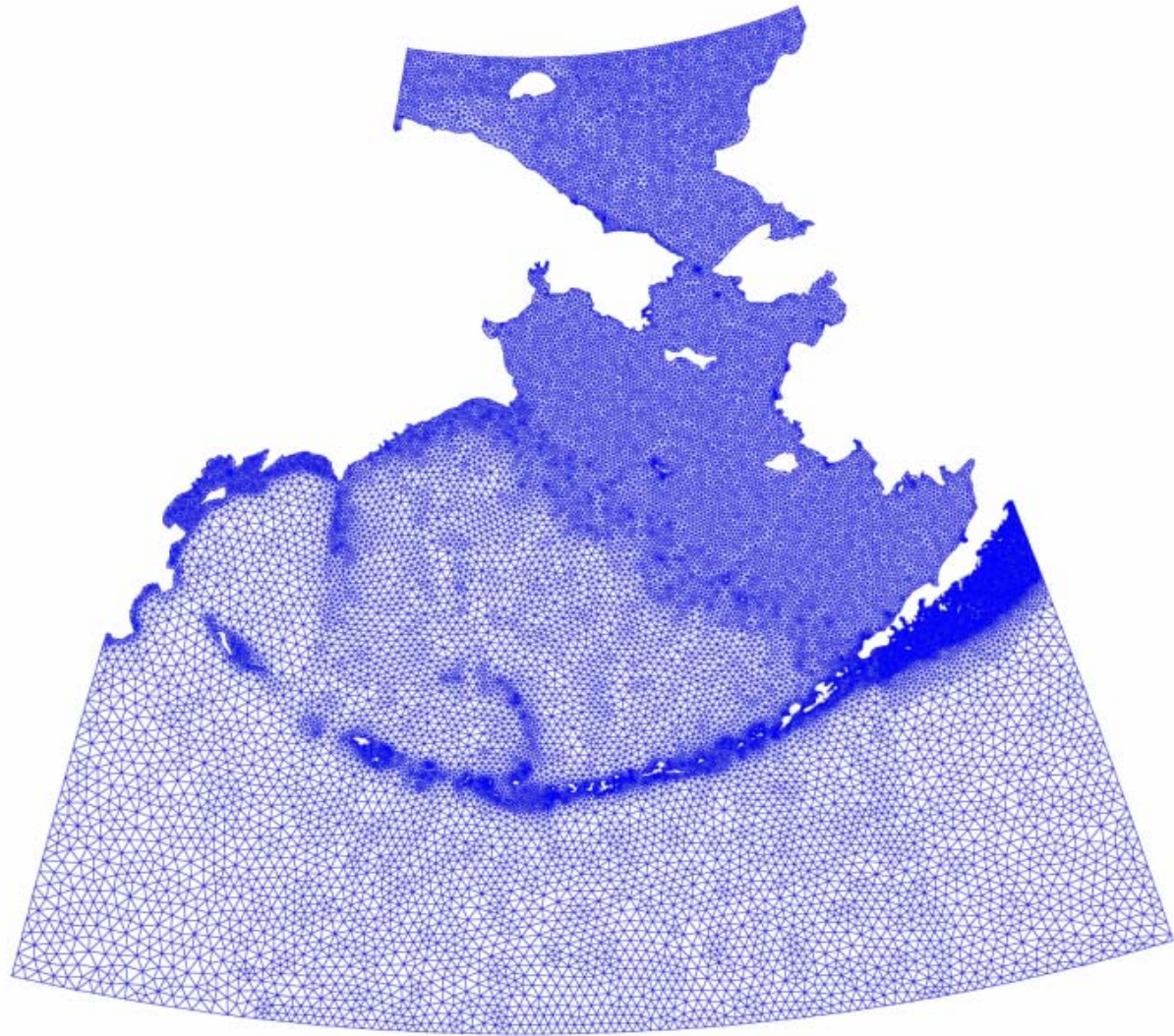
# The Numerical Techniques

- **Barotropic finite element method FUNDY5SP (Greenberg et al., 1998):**
  - linear basis functions, triangular elements
  - $e^{-i\omega t}$  time dependency,  $\omega$  = constituent frequency
  - solutions  $(\eta, u, v)$  have form  $Ae^{ig}$
  - Provides an initial solution
- **FUNDY5SP adjoint model**
  - development parallels Egbert & Erofeeva (2002)
  - representers: Bennett (1992, 2002)
  - allows improvement of initial solution by assimilating observations



# Grid & Forcing

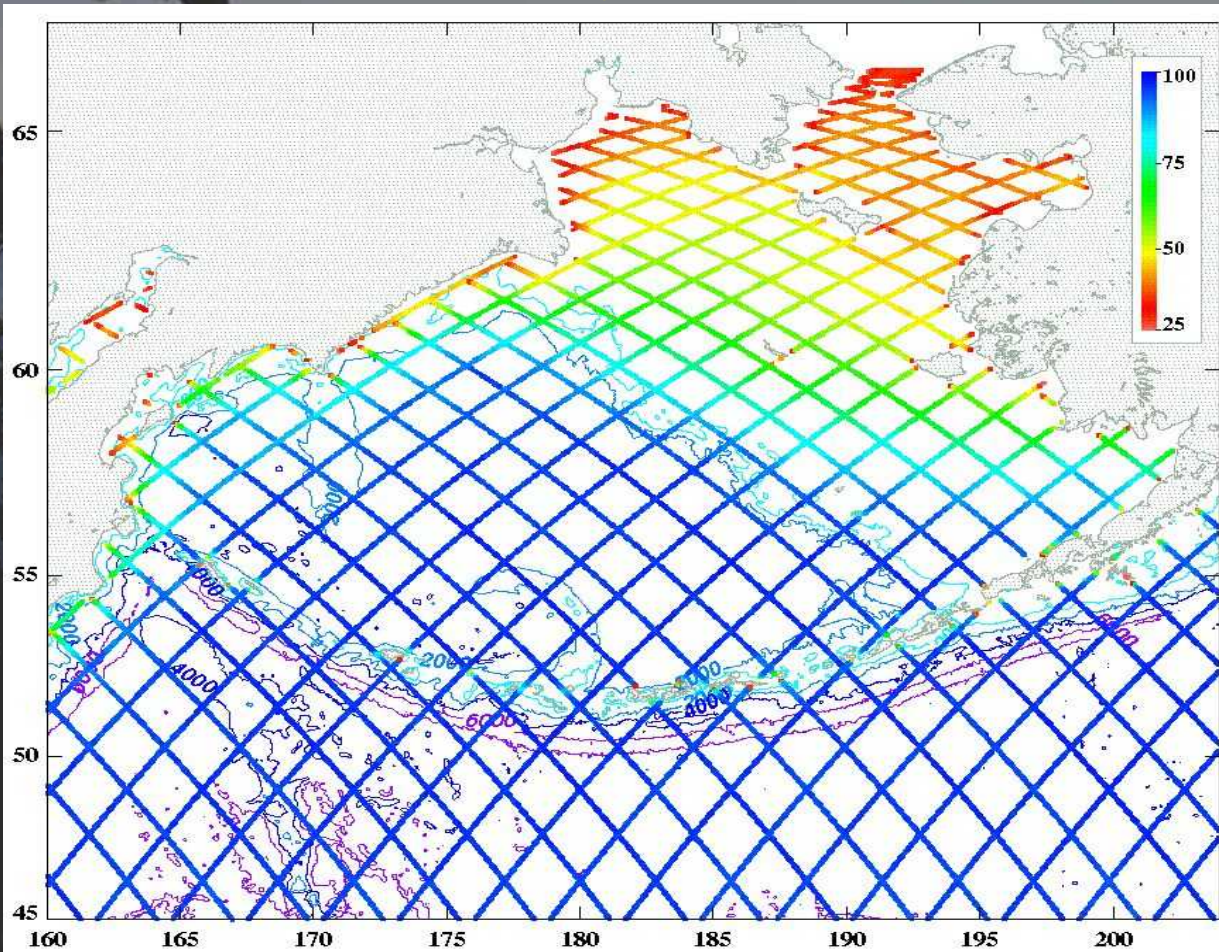
- **variable resolution:**
  - 50km to less than 1.5km
  - 29,645 nodes, 56,468 triangles
- **Forcing:**
  - Tidal elevation boundary conditions from Topex Poseidon crossover analysis
  - Tidal potential, earth tide, self-attraction & loading





# Assimilated Tidal Observations

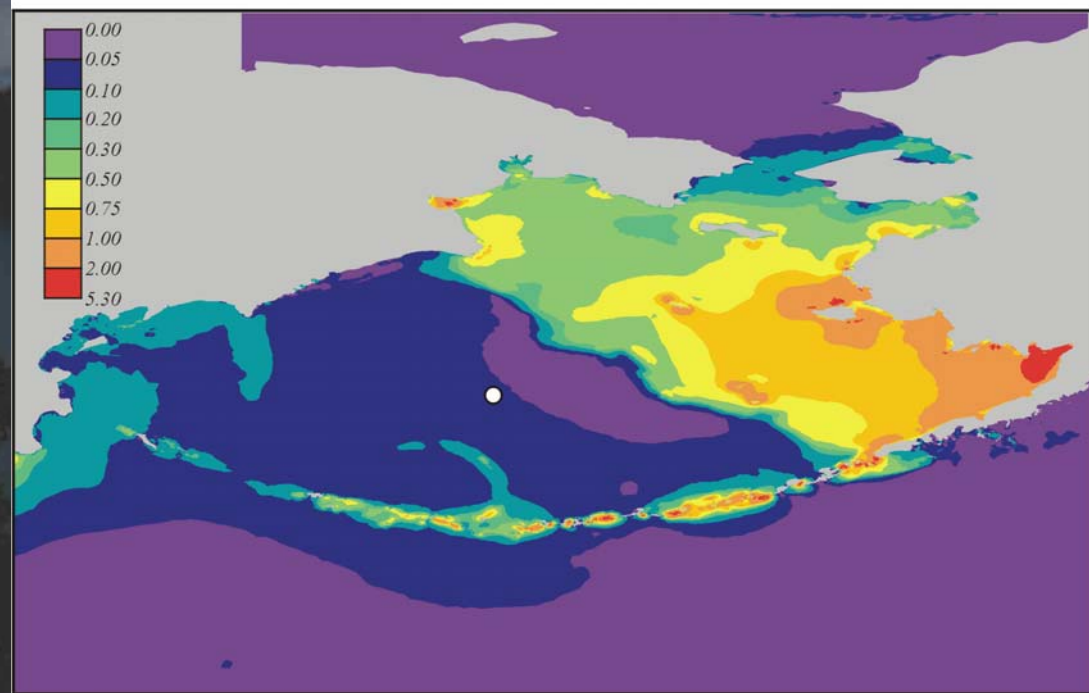
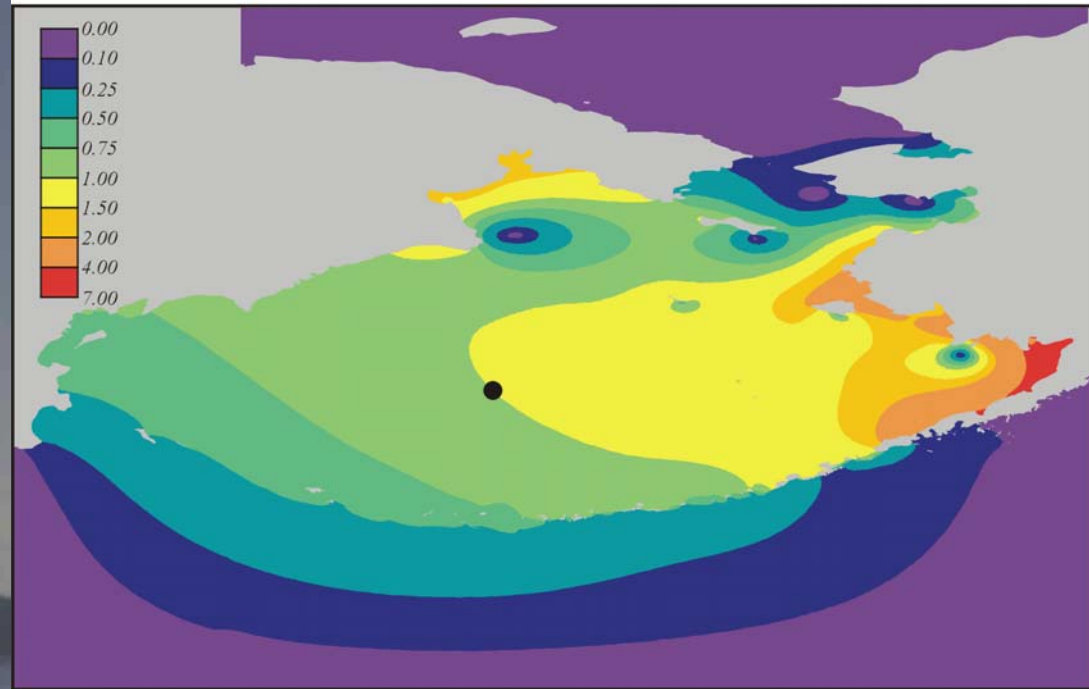
- from tidal analysis at T/P crossover sites (Cherniawsky et al. 2001)



# Elevation Amplitude & Major Semi-axis of a sample $M_2$ Representer

(amplitude normalized to 1 cm)

- these fields are used to correct  
initial model calculation





# Model Accuracy Assessment:

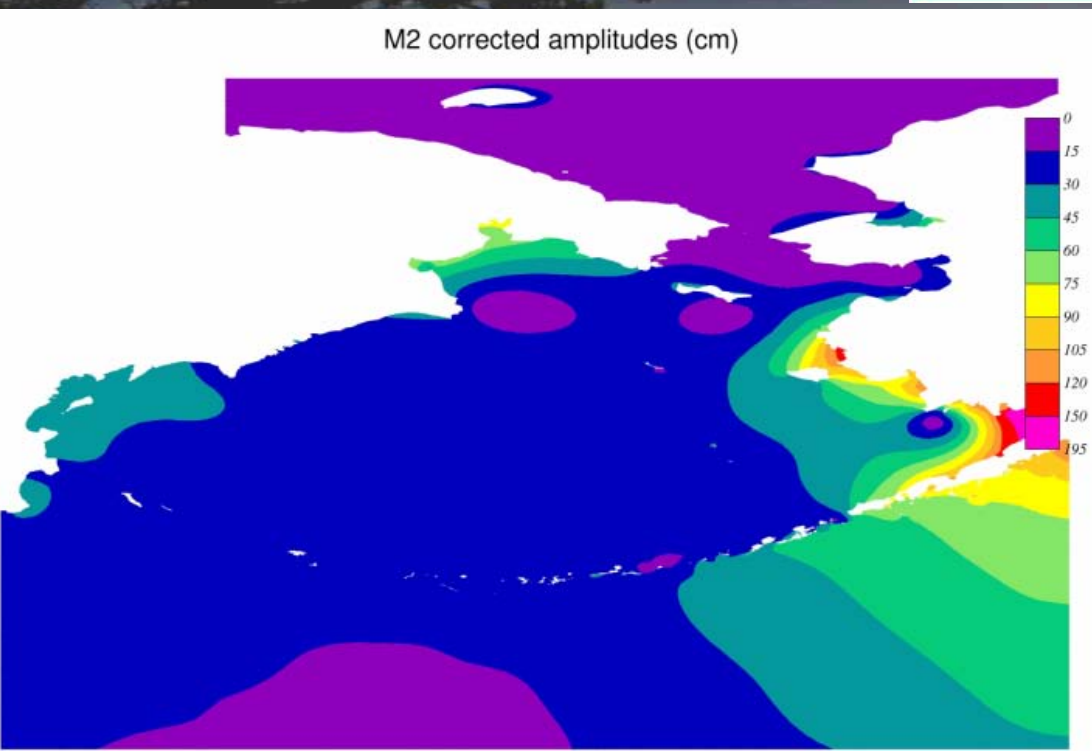
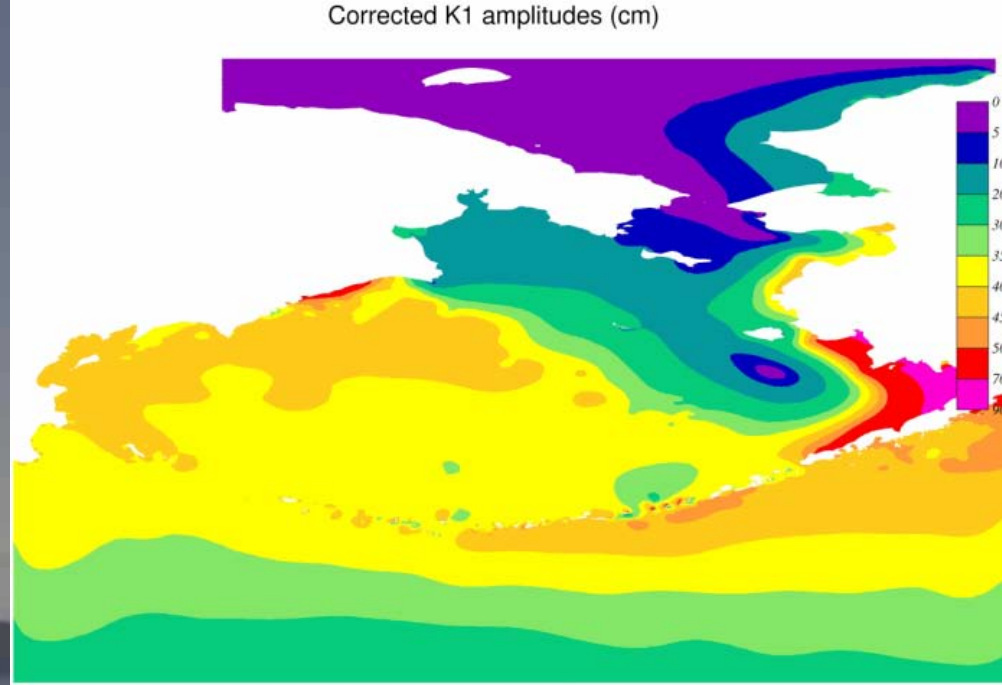
average  $D$  (cm) at 288 T/P crossover sites

$$D = \left\{ (A_0 \cos g_0 - A_m \cos g_m)^2 + (A_0 \sin g_0 - A_m \sin g_m)^2 \right\}^{1/2}$$

	M <sub>2</sub>	K <sub>1</sub>	N <sub>2</sub>	O <sub>1</sub>	S <sub>2</sub>	P <sub>1</sub>
Prior model	5.4	3.8	1.8	2.9	4.0	1.3
With T/P assimilation	2.6	2.1	1.1	1.6	1.0	1.0

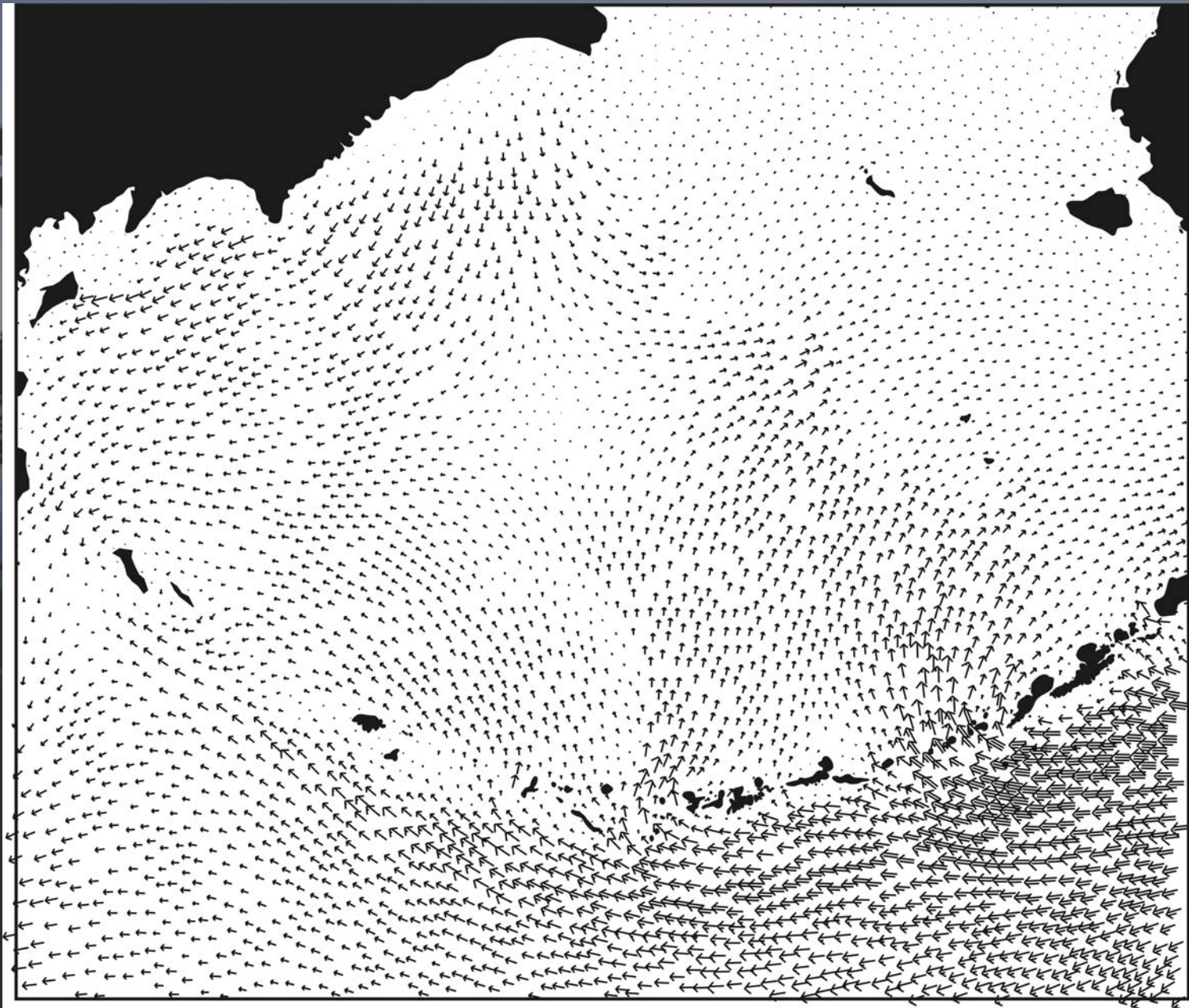


# Corrected Elevation Amplitudes



# $M_2$ vertically-integrated energy flux

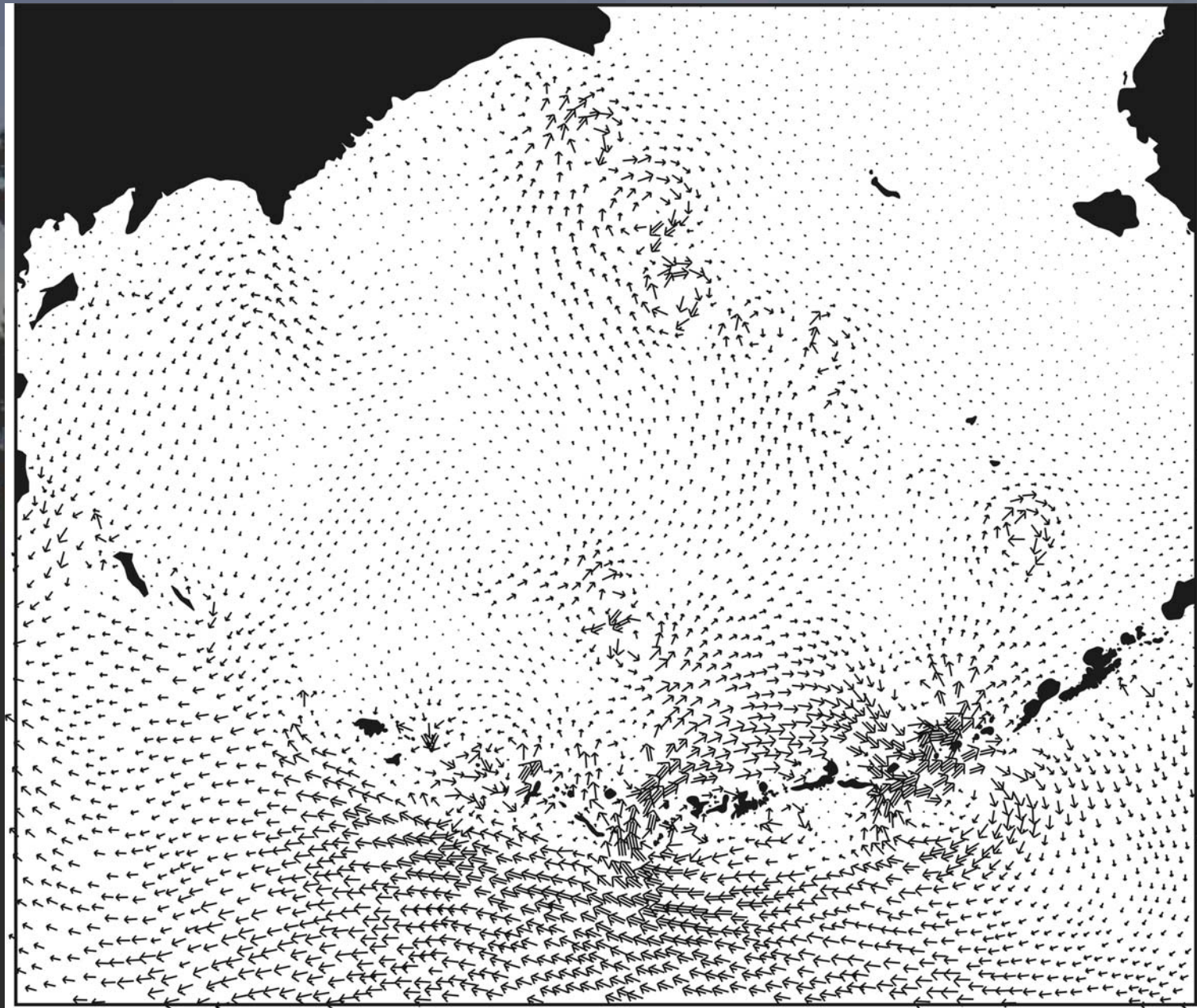
(each full shaft in multi-shafted vector represents 100KW/m)





# $K_1$ vertically-integrated energy flux

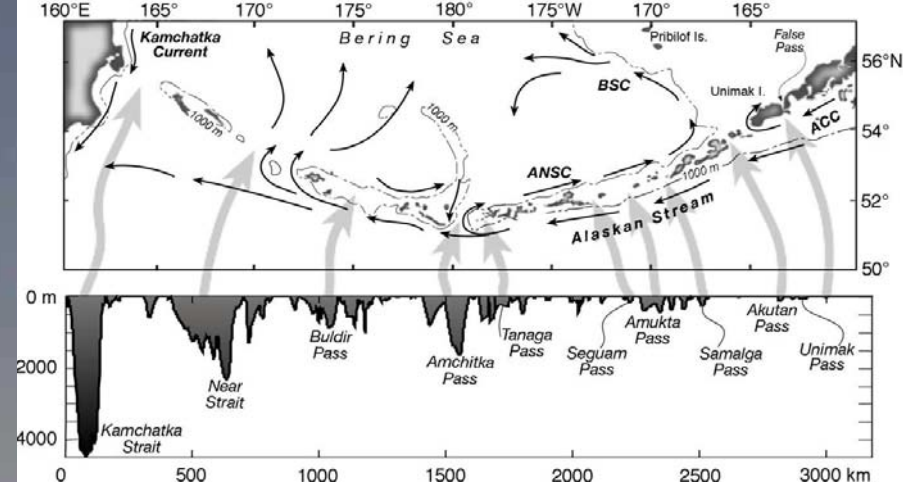
(each full shaft in multi-shafted vector represents 100KW/m)





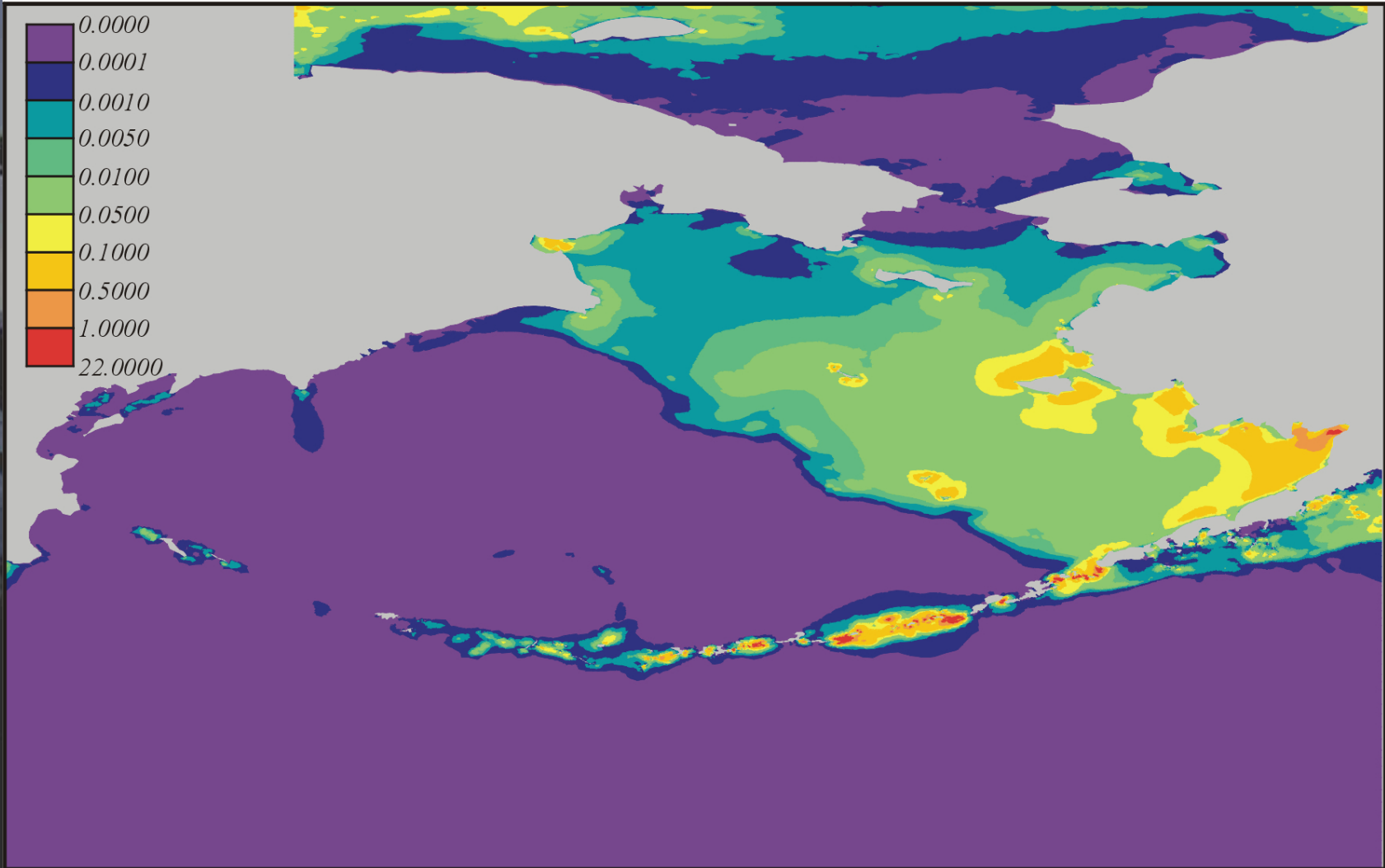
# Energy Flux Through the Aleutian Passes & Bering Strait

(Vertically integrated tidal power (GW)  
normal to transects)



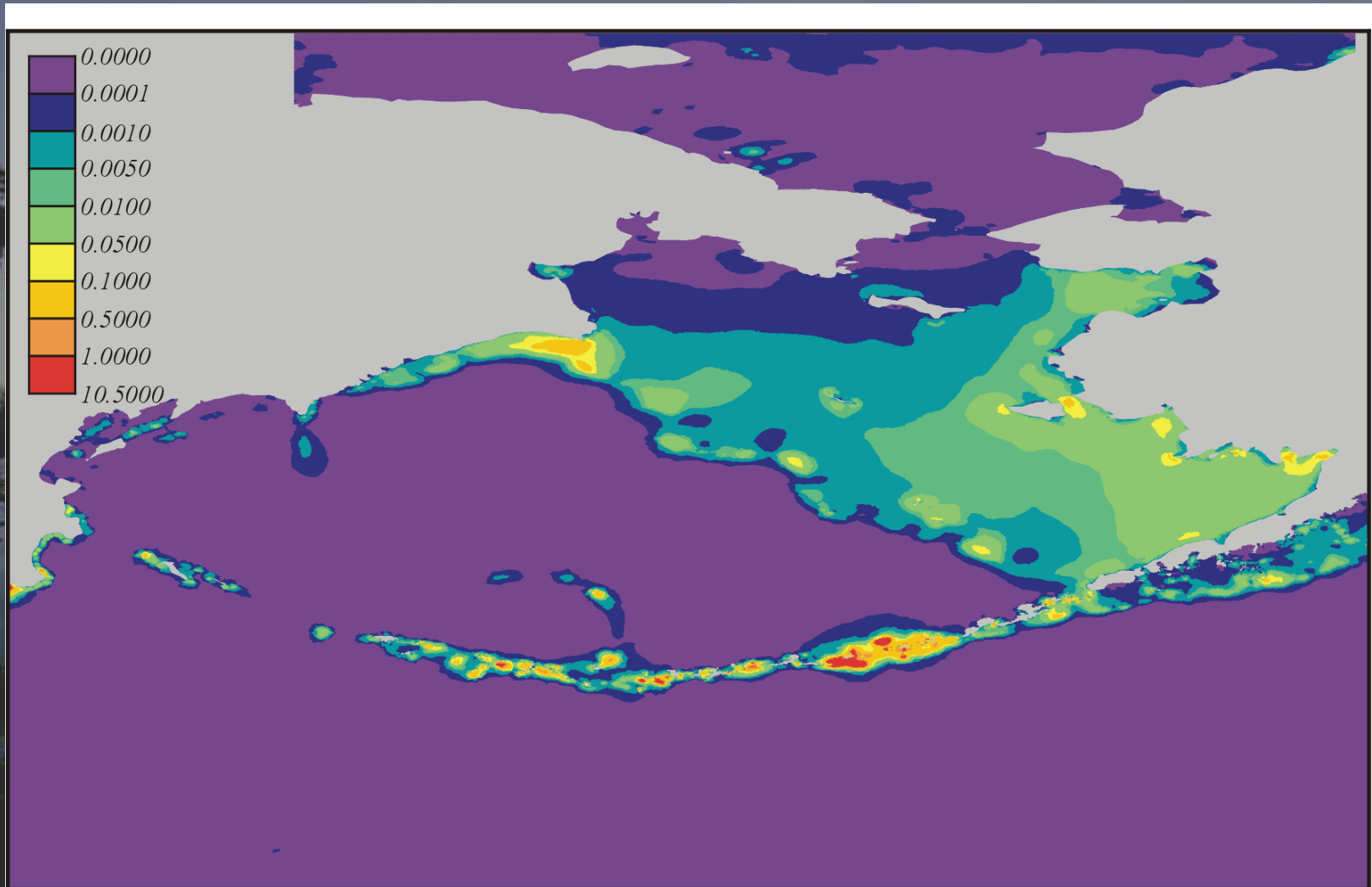
Pass(es)	M <sub>2</sub>	N <sub>2</sub>	S <sub>2</sub>	K <sub>1</sub>	O <sub>1</sub>	P <sub>1</sub>
Unimak	2.7	0.2	0.0	0.4	0.4	0.0
Akutan	1.0	0.1	0.0	0.1	0.1	0.0
Samalga	10.0	0.8	0.0	3.4	1.3	0.4
Amukta	12.5	1.1	-0.4	7.3	1.2	0.8
Seguam	1.6	0.1	-0.1	-2.7	-1.8	-0.2
Andreanof	2.1	0.2	-0.1	0.2	0.1	0.0
Tanaga	4.2	0.3	0.0	-3	-0.4	0.0
Amchitka	8.0	0.6	-0.1	22.9	12.2	2.3
Buldir	5.8	0.4	0.2	7.9	1.6	0.9
Near	-8.4	-0.2	0.0	-4.8	0.2	-0.6
Kamchatka	-8.3	-0.3	-0.4	-9.5	-1.9	-1.3
Bering Strait	0.0	0.0	0.0	0.0	0.0	0.0
<b>Total</b>	<b>31.2</b>	<b>3.3</b>	<b>-0.9</b>	<b>24.9</b>	<b>13.0</b>	<b>2.3</b>

# $M_2$ Dissipation from Bottom Friction (W/m<sup>2</sup>)



- Mostly in Aleutian Passes & shallow regions like Bristol Bay
- Bering Sea accounts for about 1% of global total of 2500 GW

# $K_1$ Dissipation from Bottom Friction ( $\text{W/m}^2$ )

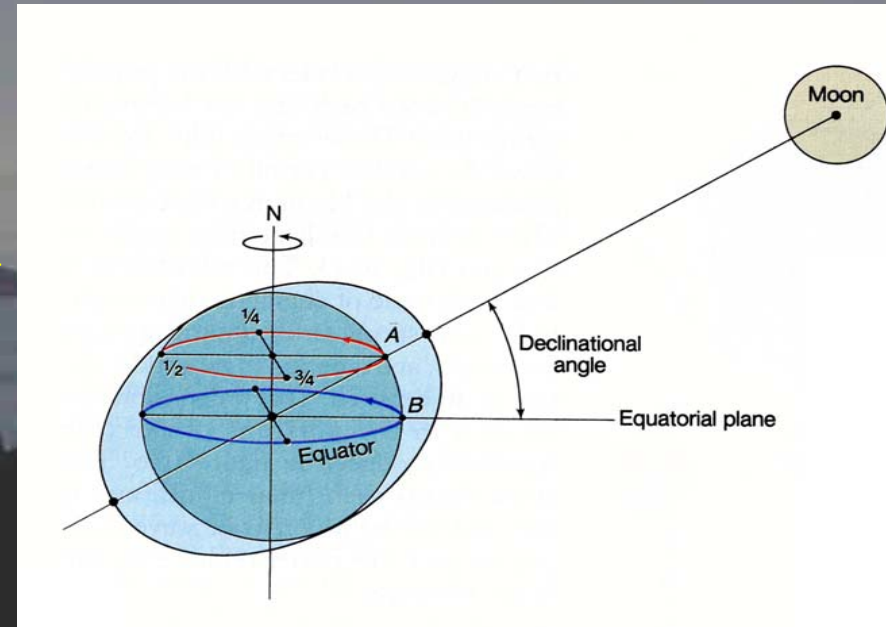


- $K_1$  dissipation mostly in Aleutian Passes, along shelf break, & in shallow regions
  - Strong dissipation off Cape Navarin as shelf waves try to turn corner
  - enhances mixing and nutrient supply → biological implications
- Bering  $K_1$  dissipation accounts for about 7% of global total of 343GW



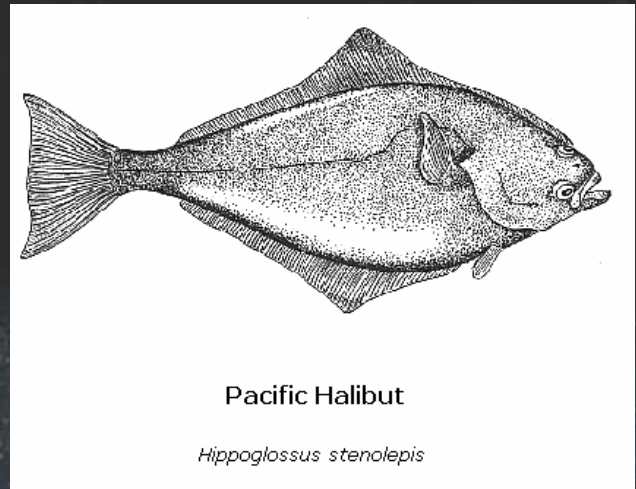
# 18.6 Year Nodal Cycle

- Declination of moons' orbit to equator varies between  $18.3^\circ$  and  $28.6^\circ$  over 18.61 year period
- leads to a small tidal constituent with 18.6 yr period & modulation of most major constituents
  - $\sim \pm 4\%$  for  $M_2$
  - $\sim \pm 13\%$  for  $K_1$
  - $\sim \pm 19\%$  for  $O_1$
- $K_1/O_1$  modulations synchronous but out of phase with  $M_2$
- $K_1/O_1$  modulations: max in 2006, min in 1997

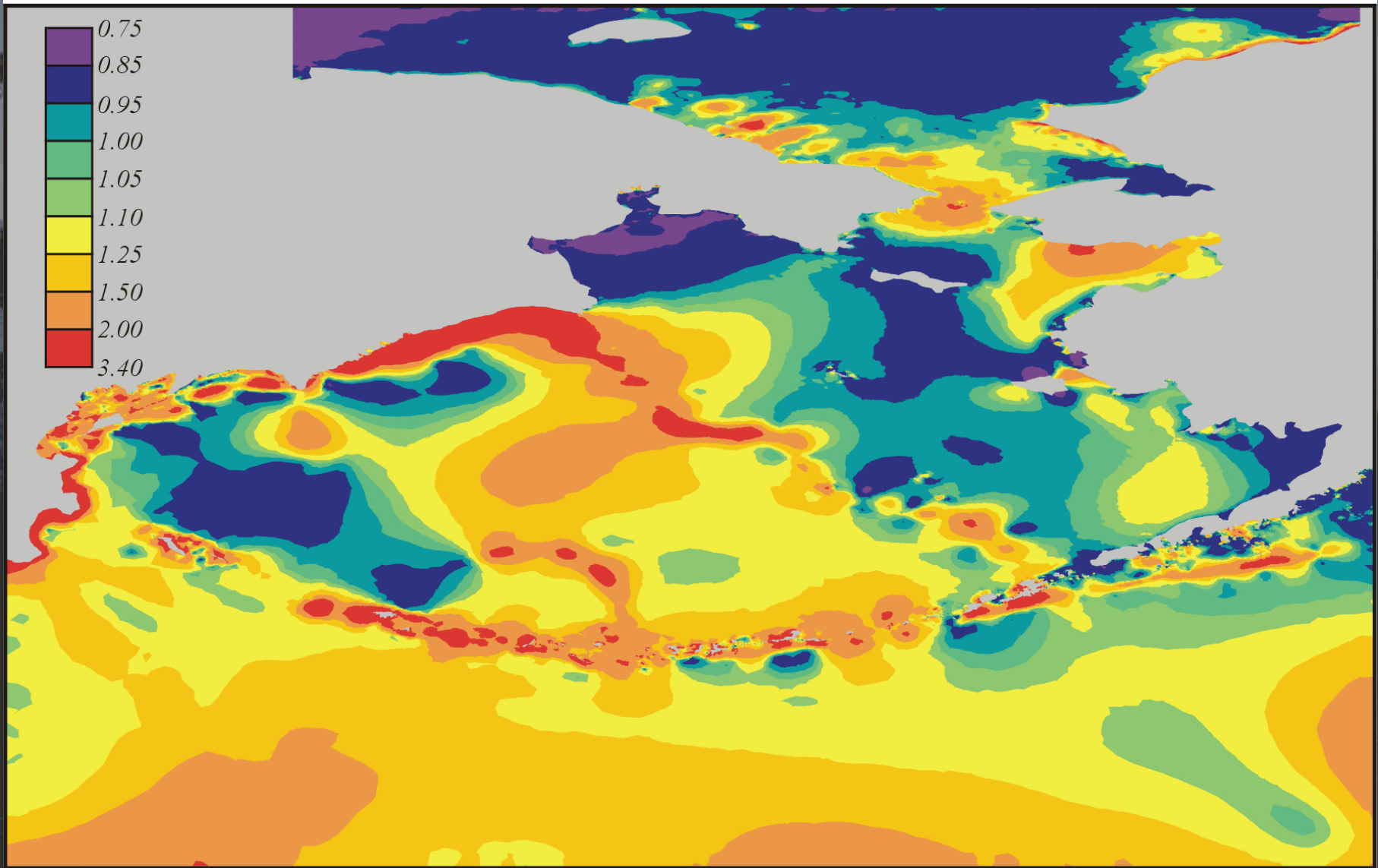


# 18.6 Year Nodal Cycle

- **Model estimates 19% increase in incoming tidal energy flux to Bering Sea from 1997 to 2006**
  - **Regional variations with relative magnitude of constituent amplitudes**
  - **36% increase in Amchitka Pass**
- **Expect variations in energy dissipation, mixing, ice cover, and biological productivity**
  - **dissipation varies as cube of velocity**
  - **Parker et al. (1995) found correlation with Pacific halibut recruitment**

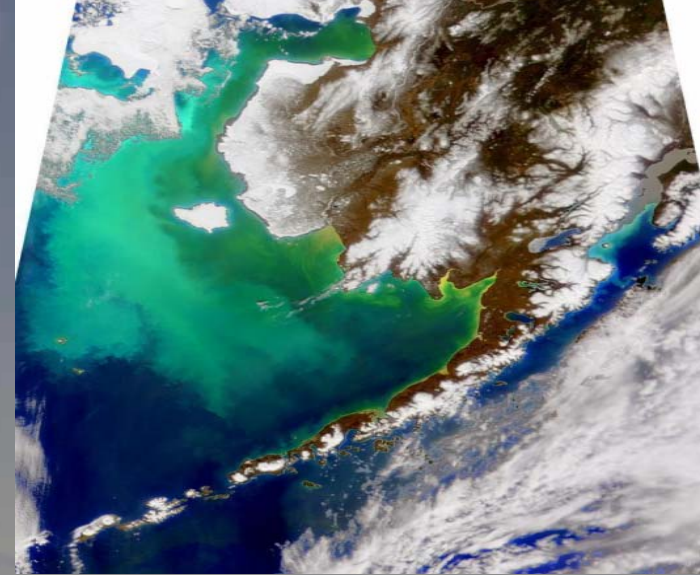


# Ratio of average bottom friction dissipation in April 2006 to that in April 1997





# Summary



- many interesting physical & numerical problems associated with tides in the Bering Sea
- representer approach is instructive way to solve the inverse problem
- 18.6 year nodal cycle
  - significant variation in energy dissipation in regions where diurnal tides dominate
  - should correlate with water properties (next speaker) & biological productivity
- More details in Foreman et al., Nov 2006 issue of *Journal of Marine Research*